## $\frac{\text { WJEC }}{\text { CBAC }}$

## GCSE MARKING SCHEME

MATHEMATICS - LINEAR
NOVEMBER 2012

## INTRODUCTION

The marking schemes which follow were those used by WJEC for the November 2012 examination in GCSE MATHEMATICS - LINEAR. They were finalised after detailed discussion at examiners' conferences by all the examiners involved in the assessment. The conferences were held shortly after the papers were taken so that reference could be made to the full range of candidates' responses, with photocopied scripts forming the basis of discussion. The aim of the conferences was to ensure that the marking schemes were interpreted and applied in the same way by all examiners.

It is hoped that this information will be of assistance to centres but it is recognised at the same time that, without the benefit of participation in the examiners' conferences, teachers may have different views on certain matters of detail or interpretation.

WJEC regrets that it cannot enter into any discussion or correspondence about these marking schemes.


\begin{tabular}{|c|c|c|}
\hline PAPER 1 (Non calculator) Foundation Tier \& Marks \& FINAL MARK SCHEME Comments \\
\hline \[
\begin{aligned}
\& \text { 6. } \begin{aligned}
\& \text { Finding the costs per pupil of tickets, bus and lunch } \\
\& \text { Cost of ticket per pupil }=915 / 98=(\text { OR } 900 / 100) \\
\&=(£) 9
\end{aligned} \\
\& \begin{aligned}
\text { Cost of bus per pupil } \& =290 / 98=(\text { OR } 300 / 100) \\
\& =(£) 3
\end{aligned} \\
\& \begin{aligned}
\text { Total cost per pupil } \& =£ 9+£ 3+£ 3.95=£ 15.95 \\
\& =\underline{(£) 16(\text { to nearest } £)}
\end{aligned}
\end{aligned}
\] \& \begin{tabular}{l}
M1 \\
A1 \\
M1 \\
A1 \\
A1
\end{tabular} \& \begin{tabular}{l}
Allow any method that implies estimating \\
Allow unsupported answers in the range 7-11 incl. \\
But if working shown then mark it. \\
Allow any method that implies estimating \\
Allow unsupported answers in the range 2-4 incl. \\
But if working shown then mark it. \\
F.T. if both Ms awarded \\
Must be rounded to the nearest \(£\)
\end{tabular} \\
\hline \begin{tabular}{l}
OR \\
Finding the TOTAL cost of tickets, bus and lunches \(/ \mathbf{9 8}\) \\
Total cost of lunches \(=(£) 3.95 \times 98=(\) OR \(£ 4 \times 100)\)
\[
=(\mathfrak{£}) 400
\] \\
Total for the trip \(=400+915+290=(\) OR \(400+900+300)\)
\[
=(\mathfrak{£}) 1600
\]
\[
\begin{aligned}
\text { Cost per pupil }=(1605 \& \text { OR } 1600) / 100 \\
\& =\underline{(£)} 16 \text { (to nearest } £)
\end{aligned}
\] \\
NOTE: \\
98~100 \\
(£)3.95~(£)4 \\
(£) 915 ~ \\
(£) 900 \\
(£)290~(£)300
\end{tabular} \& \[
\begin{aligned}
\& \text { M1 } \\
\& \text { A1 } \\
\& \text { A1 } \\
\& \text { M1 } \\
\& \text { A1 }
\end{aligned}
\] \& \begin{tabular}{l}
Allow any method that implies estimating \\
Allow estimated answers \\
F.T. if M awarded \\
Allow any method that implies estimating \\
If no marks then SC1 for any 3 of these estimates
\end{tabular} \\
\hline \begin{tabular}{l}
QWC \\
Look for \\
- Spelling \\
- Clarity of text explanations \\
- The use of notation - watch for ' \(=\) ',' \(£\) ', ' p ' being used appropriately. \\
QWC2: Candidates will be expected to \\
- present work clearly, with words explaining their processes or steps \\
AND \\
- make few if any mistakes in mathematical form, spelling, punctuation and grammar and include units in their final answer \\
QWC1: Candidates will be expected to \\
- present work clearly, with words explaining their processes or steps \\
OR \\
- make few if any mistakes in mathematical form, spelling, punctuation and grammar and include units in their final answer
\end{tabular} \& QWC
2

7 \& | QWC2 Presents relevant material in a coherent and logical manner, using acceptable mathematical form, and with few if any errors in spelling, punctuation and grammar. |
| :--- |
| QWC1 Presents relevant material in a coherent and logical manner but with some errors in use of mathematical form, spelling, punctuation or grammar. |
| OR |
| Evident weaknesses in organisation of material but using acceptable mathematical form, with few if any errors in spelling, punctuation and grammar. |
| QWC0 Evident weaknesses in organisation of material, and errors in use of mathematical form, spelling, punctuation and grammar. | <br>

\hline
\end{tabular}

| PAPER 1 (Non calculator) Foundation Tier | Marks | FINAL MARK SCHEME Comments |
| :---: | :---: | :---: |
| 7. Toronto  down 5 <br> Glasgow  -4  <br> Moscow <br> Reykjavik -7  down 4 <br>     | $\begin{gathered} \hline \text { B1 } \\ \text { B1 } \\ \text { B1 } \\ \text { B1 } \\ 4 \end{gathered}$ | If given as -5 then B0, but allow B1 if Moscow is given as -4 |
| 8. (a) Overlay <br> Plots <br> Line <br> 8. (b) Any correct strategy, e.g. 2 times value at 20 kilometres per litre $56 \times 2=112$ | P1 <br> L1 <br> M1 <br> A1 <br> 4 | A valid attempt at drawing a line/curve through the points <br> Any correct method using graph or table. <br> F.T. their graph. <br> Unsupported answers in the range 108-116 inclusive get M1, A1. |
| 9. (a)5 3 $(1$ $1)$ <br>  3 1 $(1$ <br>  $3)$   <br>  $(1$ $1)$ 3 <br>  $(1$ $3)$ 5 <br>   7  <br> (b) $\begin{array}{r} \frac{7}{16}(\text { of } 320) \\ =140 \end{array}$ <br> Cost $=320 \times 50(\mathbf{p})$ OR Prizes $=140 \times 80(\mathrm{p})$ <br> (£) 160 or 16000 <br> (p) OR <br> (£) 112 or $11200(\mathrm{p})$ $\frac{\mathbf{3 2 0} \times \mathbf{5 0}(\mathbf{p})-\text { their } \mathbf{1 4 0} \times \mathbf{8 0}(\mathbf{p})}{=£ 48 \text { OR } 4800 \text { p }}$ | B2 <br> M1 <br> A1 <br> M1 <br> A1 <br> M1 <br> A1 <br> 8 | B1 for at least 4 correct entries <br> Negative numbers are errors in this table, but follow through, if needed in part (b) <br> F.T. their table. F.T. 'their $7 / 16$ ' if a fraction less than 1 Sight of bone fide 140 in later working OR 140/320 gets M1, A1. Accept words ' 7 out of 16 ', or ' 70 out of 160 ' here. <br> For either method and accuracy for cost OR prizes. F.T. 'their 140 ' provided it is clearly identifiable. <br> A0 for £16000 OR 160p OR 112p OR £11200 <br> F.T. full method (ignore units for the M1). <br> Rounded up or down figure if their 140 is not a whole number |
| 10. (a) Base angle $=66$ $\begin{aligned} x & =180-66-66 \quad \text { OR 114-66 } \\ & =48 \end{aligned}$ <br> 10. (b) $\begin{aligned} & (180-106)=74 \\ & 360-114-53-74 \\ & =119\left(^{\circ}\right) \end{aligned}$ | $\begin{gathered} \hline \text { B1 } \\ \text { M1 } \\ \text { A1 } \\ \text { B1 } \\ \text { M1 } \\ \text { M1 } \\ \text { A } \\ \hline \end{gathered}$ | $x=66$ with no working gets B1M0A0 <br> F.T. their $180-114$ <br> For finding $4^{\text {th }}$ angle. Also look in their diagram. <br> 74 on its own gets this B1, even as $\mathrm{y}=74$ <br> Angle sum of quadrilateral. Note that $180-167+106$ is equivalent $(114+53)$ <br> F.T. 'their 74 ' |
| $\begin{aligned} & \text { 11. A }(9,5) \\ & \text { B }(26,-4) \\ & \text { C }(21,-13) \end{aligned}$ | $\begin{gathered} \text { B2 } \\ \text { B2 } \\ \text { B2 } \\ \\ \hline \end{gathered}$ | B1 for each ordinate <br> B1 for each ordinate <br> B1 for each ordinate. F.T. 'their B + (-5, -9)' |

\begin{tabular}{|c|c|c|}
\hline PAPER 1 (Non calculator) Foundation Tier \& Marks \& FINAL MARK SCHEME
Comments \\
\hline \begin{tabular}{l}
12.(a) (£)6400 \\
(b) (£) 2000 \\
(c) Reasonable straight line of best fit \\
(d) Negative (correlation) \\
(e) FT from a line of best fit (reading accurate to small square) (curved line or straight line, not dot-to-dot) H1
\end{tabular} \& \begin{tabular}{l}
B1 \\
B1 \\
B1 \\
B1 \\
B1
\end{tabular} \& \begin{tabular}{l}
Some points above and some points below \\
Do not accept from 'corner' to 'corner' of the graph paper \\
OR an answer between (£)2600 and (£)3600 inclusive if no line of best fit.
\end{tabular} \\
\hline \begin{tabular}{l}
13. (a) \(3(8 x+1)\) \\
(b) \(x(x-6)\) \\
(c) \(2 x^{4}+12 x\) \\
(d)
\[
\begin{aligned}
\mathrm{x} / 3 \& =25-15 \\
\mathrm{x} \& =30
\end{aligned}
\] \\
F13 parts (a) to (d) are H4 parts (b) to (e) \\
(e)
\[
\begin{aligned}
5 x-7 \& =3 x+6 \\
2 x \& =13 \\
x \& =6.5 \text { OR } 61 / 2
\end{aligned}
\]
\end{tabular} \& \[
\begin{gathered}
\hline \text { B1 } \\
\text { B1 } \\
\text { B2 } \\
\text { M1 } \\
\text { A1 } \\
\\
\text { B1 } \\
\text { B1 } \\
\text { B1 } \\
9
\end{gathered}
\] \& \begin{tabular}{l}
CAO \\
CAO \\
B1 for each term. If B2 penalise further wrong work -1 . \\
Or alternate correct first step \\
CAO. Accept embedded answers. Mark final answer. \\
SC1 for \(\mathrm{x}=120\) from \(\mathrm{x} / 3=40\), OR \\
SC1 for 'ladder method' showing \(-15, \times 3\) \\
FT until \(2^{\text {nd }}\) error \\
OR \(x=13 / 2\) \\
Must be simplified \\
SC1 for 'ladder method'
\end{tabular} \\
\hline \begin{tabular}{l}
14.(a) Strategy, shorter edges meeting (accept a diagram) (Showing) 6 on longer sides ( 2 lots of 3 ) and 1 on each end OR idea end tables seat 7 people and middle table seat 6 people (Number of tables is) \((164-2) \div 6\) \\
OR 2 correct trials with equivalent " \(\times 6+2\) " 27 (tables) \\
(b) \((\mathrm{n}-2) \div 6\) OR \((\mathrm{n}-2) / 6\) \\
H5
\end{tabular} \& \(\begin{array}{r}\text { S1 } \\ \text { M1 } \\ \text { M1 } \\ \text { A1 } \\ \\ \hline\end{array}\) \& \begin{tabular}{l}
May be implied in later working that this is the arrangement \\
Accept intention, not about notation SC2 for 79 or SC1 for ( \(164-6\) )/2 \\
Alternative: \\
Any 3 multiples of 6 shown or3 terms of a sequence \\
going up in 6s, or 164/6 or 164 \(\div 6\) \\
\(27 \times 6=162\) OR 27 remainder 2 OR 27.3(3..) M1 \\
(this implies S1 also) \\
\(162+2=164\) (seen or implied) \\
27 (tables) \\
An answer of 27 from working ' 27 remainder 2' or '27.3(3..)' must be confirmed in order to award the final M1, A1 ( i.e. remainder justified), otherwise SC1 instead An answer of 27 (tables) without working is awarded SC3 \\
FT misunderstanding longer edges joined leading to ( \(n-6\) ) \(\div 2\) \\
B2 for \(n-2 \div 6\) or \(n-2 / 6\) or \(-2 \div 6\) \\
B1 for -2 or \(\div 6\) in an expression or \(n=6 \times t a b l e s+2\), or \(n=6 \times t+2\) \\
B0 for \(\times 6+2\) or \(n \times 6+2\)
\end{tabular} \\
\hline \begin{tabular}{l}
15. Realising could be \(2+2,1+3,3+1\) \\
Realising 36 different outcomes OR sight of \(1 / 6 \times 1 / 6\) \\
OR product of 2 terms both with denominators of \(\mathbf{6}\) seen \\
OR sight of a denominator of 36 \\
\(3 / 36\) or equivalent \\
H6
\end{tabular} \& B1
B1

B1

3 \& | May be within a sample space diagram, e.g. sight of twoway table with three 4 s shown, or the appropriate additions |
| :--- |
| Maybe shown in a sample space diagram with indication of 36, must be stated not implied |
| Ignore incorrect cancelling | <br>

\hline | 16. |
| :--- |
| Middle card 6 |
| Two cards (or three cards) 3 as the mode for their cards |
| First card 1 and last card 9 (or in reverse) |
| Correct answer 1336789 or in reverse H7 | \& \[

$$
\begin{gathered}
\text { B1 } \\
\text { B1 } \\
\text { B1 } \\
\\
\text { B1 } \\
4 \\
\hline
\end{gathered}
$$

\] \& | If boxes are blank, mark the working |
| :--- |
| Smaller numbers to one side and larger to the other 3 is the distinct mode for their cards OR any pair of single digit numbers (including negatives) with a difference of 8 CAO | <br>

\hline
\end{tabular}

PAPER 1 - HIGHER TIER


\begin{tabular}{|c|c|c|}
\hline PAPER 1 Higher Tier \& Marks \& FINAL MARK SCHEME Comments \\
\hline \begin{tabular}{l}
5.(a) Strategy, shorter edges meeting (accept a diagram) (Showing) 6 on longer sides ( 2 lots of 3 ) and 1 on each end \\
OR idea end tables seat 7 people and middle table seat 6 people \\
(Number of tables is) \((164-2) \div 6\) \\
OR 2 correct trials with equivalent " \(\times 6+2\) " 27 (tables)
\end{tabular} \& S1
M1

M1

A1 \& | May be implied in later working that this is the arrangement |
| :--- |
| Accept intention, not about notation. |
| For a complete correct method that could lead to 27 tables |
| SC2 for 79 or 54 , or SC1 for $(164-6) / 2$ |
| Alternative: |
| Any 3 multiples of 6 shown or 3 terms of a sequence going |
| up in $6 s$, or $164 / 6$ or $164 \div 6 \quad$ Sl |
| $27 \times 6=162$ OR 27 remainder 2 OR 27.3(3..) M1 |
| (this implies S1 also) |
| $162+2=164$ (seen or implied) M1 |
| 27 (tables) |
| An answer of 27 from working ' 27 remainder 2' or |
| '27.3(3..)' must be confirmed in order to award the final | <br>

\hline \& QWC \& An answer of 27 (tables) without working is awarded SC3 <br>

\hline | QWC2: Candidates will be expected to |
| :--- |
| - present work clearly, maybe with diagrams and words explaining process or steps |
| AND |
| - make few if any mistakes in mathematical form, spelling, punctuation and grammar and include units in their final answer |
| QWC1: Candidates will be expected to |
| - present work clearly, maybe with diagrams and words explaining process or steps |
| OR |
| - make few if any mistakes in mathematical form, spelling, punctuation and grammar and include units in their final answer | \& \& | QWC2 Presents relevant material in a coherent and logical manner, using acceptable mathematical form, and with few if any errors in spelling, punctuation and grammar. |
| :--- |
| QWC1 Presents relevant material in a coherent and logical manner but with some errors in use of mathematical form, spelling, punctuation or grammar OR evident weaknesses in organisation of material but using acceptable mathematical form, with few if any errors in spelling, punctuation and grammar. |
| QWC0 Evident weaknesses in organisation of material, and errors in use of mathematical form, spelling, punctuation or grammar. | <br>


\hline (b) ( $\mathrm{n}-2) \div 6$ OR $(\mathrm{n}-2) / 6$ OR equivalent \& B3 \& | FT misunderstanding longer edges joined leading to ( $n$ 6) $\div 2$ |
| :--- |
| B2 for $\mathrm{n}-2 \div 6$ or $\mathrm{n}-2 / 6$ or $-2 \div 6$ |
| B1 for -2 or $\div 6$ in an expression |
| or $\mathrm{n}=6 \times$ tables +2 , or $\mathrm{n}=6 \times \mathrm{t}+2$ |
| B0 for $\times 6+2$ or $\mathrm{n} \times 6+2$ | <br>

\hline 6. Realising could be $2+2,1+3,3+1$ \& B1 \& <br>
\hline Realising 36 different outcomes OR sight of $1 / 6 \times 1 / 6$ OR product of 2 terms both with denominators of 6 seen OR sight of a denominator of 36 $3 / 36$ or equivalent \& B1

B1

3 \& | Maybe shown in a sample space diagram with indication of 36 , must be stated not implied |
| :--- |
| Ignore incorrect cancelling | <br>

\hline
\end{tabular}

| PAPER 1 <br> Higher Tier | Marks | FINAL MARK SCHEME |
| :---: | :---: | :---: |
| 7. <br> Middle card 6 <br> Two cards (or more) 3 as the mode for their cards First card 1 and last card 9 (or in reverse) <br> Correct answer 1336789 or in reverse | $\begin{gathered} \text { B1 } \\ \text { B1 } \\ \text { B1 } \\ \\ \text { B1 } \\ 4 \end{gathered}$ | If boxes are blank, mark the working Smaller numbers to one side and larger to the other 3 is the distinct mode for their cards OR any pair of single digit numbers (including negatives) with a difference of 8 CAO |
| 8.(a) 3 reasonable rounded values which could lead to simple calculations <br> Correct evaluation for their figures <br> (b) 3.45 <br> (c) $3 / 16$ <br> (d) 2, 2, 2, 2, 3, 5 $2^{4} \times 3 \times 5$ <br> (e) $1 / 0.9$ or $1 /(9 / 10)$ or $10 / 9$ <br> 10/9 and indication that this is GREATER than 0.9 | M1 A1 B1 B1 B2 B1 M1 A1 9 | Not all 3 need to be different to those given <br> (Common responses include 5 here) <br> CAO <br> Allow 0.1875. Do not accept 1.5/8 <br> B1 for at least 2 correct primes before $2^{\text {nd }}$ error <br> FT "their" primes, needs to have at least 1 index $>1$ <br> Or $1^{1}{ }^{1}$ or $1.1(11 .$.$) , statement in reverse$ |
| 9.(a) $6 x^{2}+15 x-8 x-20$ $=6 x^{2}+7 x-20$ <br> (b) $(2 x+3)(x-1)$ <br> Both possible solutions $\mathrm{x}=-3 / 2$ AND $\mathrm{x}=1$ <br> (c) $(x+5)^{6}$ <br> (d) $\mathrm{n}^{2}+4$ or equivalent | $\begin{gathered} \text { B2 } \\ \text { B1 } \\ \\ \text { B2 } \\ \text { B1 } \\ \text { B1 } \\ \text { B2 } \\ 9 \end{gathered}$ | B1 for any 3 terms correct FT from B1 provided collection required. Mark final answer <br> SC1 for an answer of $6 x^{2}(\ldots)-20$ <br> B1 for ( 2 x .. 3 )( x .. 1 ) or ( 2 x .. 1 )(x .. 3 ) <br> FT from their pair of brackets <br> CAO. Mark final answer <br> B1 for (1) $\mathrm{n}^{2} \pm \ldots$, not for $\mathrm{n}^{2}$ alone |
| 10.(a) All entries correct <br> (b) $0.7 \times 0.7$ $0.49$ | $\begin{gathered} \text { B2 } \\ \text { M1 } \\ \text { A1 } \\ 4 \end{gathered}$ | B1 for any one pair of branches correct FT from their tree, provided numbers >0 and <1 |
| 11.(a) Initial strategy, e.g. sketch of concentric rectangles Correct method to find area, e.g. subtraction of areas or composite shapes $\begin{gathered} (9+2 x)(5+2 x)-9 \times 5 \text { or } 9 x+9 x+5 x+5 x+x^{2}+x^{2}+x^{2}+x^{2} \\ 4 x^{2}+28 x \text { or } 4\left(x^{2}+7 x\right) \text { or } 4 x(x+7) \end{gathered}$ <br> (b) Strategy, drawing with $1 / 4$ circles in corners OR sight of $\pi x^{2}$ of a fraction or multiple of $\pi x^{2}$ (or equivalent) | S1 <br> M1 <br> A1 <br> A1 <br> S1 <br> M1 <br> A1 <br> 7 | For intention, but some sections may be missed <br> Or equivalent <br> Mark final answer <br> If the path has been built inside then MR-1 and FT (leading <br> to $28 x-4 x^{2}$ ) <br> FT from (a), to give their (a) $-4 x^{2}+\Pi x^{2}$, <br> Not for sight of $\pi r^{2}$ <br> Mark final answer <br> If the path has been built inside then MR-1 and FT |
| 12.(a) -5 and -12 <br> (b) Any 6 correct plots <br> All 8 correct plots joined with a smooth curve <br> (c) 2 and 6 <br> (d) y values $0,3,4,3,0$ <br> Split correct region into areas to sum <br> Numerically correct area calculations shown 10 (square units) | $\begin{gathered} \text { B2 } \\ \text { B1 } \\ \text { B1 } \\ \text { B1 } \\ \text { B1 } \\ \text { M1 } \\ \text { A1 } \\ \text { A1 } \\ 9 \end{gathered}$ | B1 for each correct answer <br> FT from (a) <br> FT from (a) <br> Coordinate notation is not required. <br> Accept embedded answers <br> Sight of these values alone or within a calculation <br> FT for 1 incorrect y value only. <br> May included area below x -axis $(1 / 2(3)+1 / 2(3+4)+1 / 2(4+3)+1 / 2(3))$ <br> ( +60 if below x -axis included <br> CAO |
| $\text { 13. } \begin{gathered} \mathrm{y} \propto 1 / \mathrm{x}^{2} \text { OR } \mathrm{y}=\mathrm{k} / \mathrm{x}^{2} \\ 10=\mathrm{k} / 12^{2} \\ \mathrm{y}=1440 / \mathrm{x}^{2} \end{gathered}$ | $\begin{gathered} \mathrm{B} 1 \\ \mathrm{M} 1 \\ \text { A1 } \\ 3 \end{gathered}$ | Ignore use of incorrect symbol ' $\alpha$ ' later FT y $\alpha 1 / \mathrm{x}$ or $\mathrm{y} \alpha \mathrm{x}^{2}$ for possible M1, A1 |


| PAPER 1 <br> Higher Tier | Marks | FINAL MARK SCHEME Comments |
| :---: | :---: | :---: |
| 14.(a) Transformation horizontally to the right Correct translation with 2 indicated correctly on the x -axis <br> (b) Idea of reflection in x -axis <br> Idea of vertical translation <br> Correct transformation with 3 indicated on the $y$-axis | $\begin{gathered} \hline \text { B1 } \\ \text { B1 } \\ \text { B1 } \\ \text { B1 } \\ \text { B1 } \\ 5 \end{gathered}$ | SC1 for left shift with -2 indicated on the x -axis <br> May include an incorrect translation, but clearly there has been a reflection <br> Allow 'up' or 'down' |
| 15.(a) $1 / 8000$ <br> (b) Attempt to subtract $100 x=65.252 \ldots$ and $x=0.652 \ldots$ <br> (c) $9-15 \sqrt{ } 2-15 \sqrt{ } 2+50$ $\begin{gathered} =59-30 \sqrt{ } 2 \\ \text { Irrational } \end{gathered}$ | $\begin{gathered} \hline \text { B2 } \\ \text { M1 } \\ \text { A1 } \\ \text { M1 } \\ \text { A1 } \\ \text { B1 } \\ 7 \\ \hline \end{gathered}$ | ```B1 for \(1 / 20^{3}\) Or equivalent for 1000 \(x-10 x\) Final answer of 64.6/99 M1 only With at least 3 of the terms correct OR \(9 \pm \mathrm{a} \sqrt{2}+50\) with \(\mathrm{a} \neq 0\) CAO FT provided at least M1 awarded``` |
| 16.(a) Any one correct area $10+15+35+80$ $=140$ <br> (b) (i) 50 (seconds) <br> (ii) Correct histogram <br> (c) A reasonable statement, <br> e.g. 'No, children median lower', or 'no, 140 children less than 50 seconds but only 100 adults', or 'no, because more adults spent over 50 seconds' | B1 <br> M1 <br> A1 <br> B1 <br> B3 <br> E1 <br> 8 | $10,15,35,80,60$ <br> If no other marks allow SC 1 for an answer of 135 <br> Do not accept a group or interval <br> B2 for sight of 1, 2, 2.5, 3.5, 10 or histogram with first bar correct but with 1 error in one of the other bars, OR B1 for histogram with any 3 bars correct Could be either Yes or No with a suitable reason. FT their histogram Accept an answer of 'same' if the candidate calculating the means to be the same |

PAPER 2 - FOUNDATION TIER

\begin{tabular}{|c|c|c|}
\hline PAPER 2 (Calculator allowed) Foundation Tier \& Marks \& FINAL MARK SCHEME Comments \\
\hline \begin{tabular}{l}
1. (a) \begin{tabular}{ccl} 
(242.68) \& \\
\& 146.16 \& (tables) \\
\& \(87.5(0)\) \& (chairs) \\
\& \& 160.56
\end{tabular} (cabinets) \\
(£) \(636.9(0)\) \\
(b) Builder pays (£) 573.21
\end{tabular} \& \begin{tabular}{l}
B1 \\
B1 \\
B1 \\
B1 \\
B2 \\
6
\end{tabular} \& \begin{tabular}{l}
F.T. their figures for 1 error \\
F.T. their total rounded or truncated. Must be in 2 dec. places for the \(\mathbf{B 2}\) \\
B1 for a correct \(10 \%\) (f) 63.69 . \\
\(\underline{2 \text { dec. } p l \text {. NOT required for B1 }}\)
\end{tabular} \\
\hline  \& \begin{tabular}{l}
B1 \\
B1 \\
B1 \\
B1 \\
4
\end{tabular} \& \\
\hline \begin{tabular}{l}
3. (a) Evidence of square counting \(72-78\) (inclusive) \\
3. (b) Lines \\
Arc \\
3. (c) c \\
a \\
b
\end{tabular} \& \[
\begin{gathered}
\hline \text { M1 } \\
\text { A1 } \\
\text { B1 } \\
\text { B1 } \\
\text { B1 } \\
\text { B1 } \\
\text { B1 } \\
7 \\
\hline
\end{gathered}
\] \& \begin{tabular}{l}
Correct curvature starting and ending at the candidate's 2 lines. \\
If angle values used then they must be appropriate on the diagram AND in the correct place on the answer line.
\end{tabular} \\
\hline \begin{tabular}{l}
4. (a) Spring (S) 10, Summer (U) 15, Autumn (A) 8, Winter (W) 7 \\
Both axes labelled, e.g. frequency along one axis and Spring (S), Summer (U), Autumn (A), Winter (W) along other axis (or on the bars) \\
Anywhere within the base (inc.) of the corres. bar. and uniform scale for the frequency axis starting at 0 and labelled 'frequency' OR 'number of pupils'.
\end{tabular} \& B2
B2 \& \begin{tabular}{l}
May be inferred from their bar chart. \\
B1 for any two/three correct frequencies \\
If frequencies score 0 , then give B1 for all 4 correct tallies. \\
B1 if no scale, but allow one square to represent 1 \\
OR B1 if not labelled as 'frequency' or similar. \\
If frequency scale starts with 1 at the top of the first square the starting at 0 will be implied for this axis. \\
Condone frequency numbers alongside square instead of at the top of the squares.
\end{tabular} \\
\hline Four bars at correct heights (bars must be of equal width). Can be in any order. \& B2 \& \begin{tabular}{l}
F.T. their frequencies throughout. \\
B1 for any 2 or 3 correct bars on F.T. \\
If no frequencies given in their working, penalise -1 for each incorrect frequency on their bars up to -4 (First and third B2s)
\end{tabular} \\
\hline (b) Summer OR U \& B1 \& Accept 15 and (Summer OR U), but B0 for 15 only \\
\hline (c) \(7 / 40 \quad\) I.S.W. \& \(B 2\)

9 \& | B1 for the 7 (in a fraction < 1) OR B1 for a denominator of 'their 40' (in a fraction < 1). F.T. their frequencies. |
| :--- |
| Penalise -1 for incorrect notation, e.g. ' 7 out of 40 ', ‘ $7: 40$ ' Allow decimals and percentages including on F.T. For example, (0). 175 or $17.5 \%$ for $7 / 40$ | <br>

\hline
\end{tabular}

| PAPER 2 (Calculator allowed) Foundation Tier | Marks | FINAL MARK SCHEME Comments |
| :---: | :---: | :---: |
| 5. (a) <br> (b) likely | B1 <br> B1 <br> B1 <br> B1 <br> 4 | A should be between $1 / 2$ and $3 / 4$ (Accept $\mathbf{P}$ for $\mathbf{A}$ ). <br> A should be to the right of the halfway and up to alongside the gap between the a and $l$ in ball (OR between ê and $l$ in pêl in the Welsh version) B should be at 1 . <br> C should be between 0 and $1 / 4 \quad$ (Accept $\mathbf{G}$ for $\mathbf{C}$ ). <br> $C$ should be to the right of the 0 and up to alongside the $y$ in probability (OR the $y$ in tebygolrwydd in the Welsh version) |
| $6 . \quad(1 / 4)$ $\frac{(0) .25}{}$ $(25 \%)$ <br> any fraction equiv. to $6 / 10$ $(0.6)$ $\underline{60(\%)}$ <br> $\underline{\text { any fraction equiv. to } 3 / 4}$ $(0.75)$ $(75 \%)$ | $\begin{gathered} \text { B1 } \\ \text { B1, B1 } \\ \text { B1 } \\ 4 \\ \hline \end{gathered}$ | ISW for the fractions $6 / 10$ and $3 / 4$ Do not accept fractions like 7.5/10 |
| All triangles must be 'base' side to 'base' side <br> 7. (a) Rhombus OR square <br> Sketch <br> 7. (b) Kite <br> Sketch | B1 <br> B1 <br> B1 <br> B1 <br> 4 | Mark name first then sketch <br> B0 for what looks more like a parallelogram than rhombus <br> Mark name first then sketch |
| 8. (a) (i) Decrease previous term by 7 <br> (ii) Multiply previous term by -2 <br> 8. (b) (i) 10 w <br> (ii) $x-6$ and $x+6$ | $\begin{aligned} & \text { B1 } \\ & \text { B1 } \\ & \text { B1 } \\ & \text { B1 } \end{aligned}$ | Accept -7. <br> Accept $\times-2$$\quad \underline{\text { B0 for } \mathbf{n}-\mathbf{7}}$Allow $\mathbf{1 0} \times \mathbf{w}, \mathbf{w} \times \mathbf{1 0} \times \mathbf{\text { and } \mathbf { w 1 0 }}$.Ignore $\mathbf{w}=\mathbf{a n d} \mathbf{~}=\mathbf{w}$For both |
| 8. (c) $1 / 9 \times 45=5$ and $4 \times 5$ $=20$ | $\begin{gathered} \text { M1 } \\ \text { A1 } \end{gathered}$ | Any correct method |
| 8. (d) $5 \times 4=2 \mathrm{P}+3 \times-4$ $\begin{aligned} 2 \mathrm{P} & =20+12 \text { OR } 32 \\ \mathrm{P} & =16 \end{aligned}$ | $\begin{aligned} & \text { B1 } \\ & \text { B1 } \\ & \text { B1 } \end{aligned}$ | Correct substitution, not awarded until the 2 multiplications are seen to be implemented. Sight of $\mathbf{2 0}$ and $\mathbf{- 1 2}$ gets B1 F.T. <br> $\mathrm{P}=32 / 2$ gets B 0 . Must be 16 <br> F.T. $\mathrm{P}=$ 'their 32 ' $/ 2$. <br> Allow embedded answers, such as $20=2 \times 16-12$. |
| $\begin{aligned} & \text { 8. (e) } 4 x=18 \\ & (x=) 41 / 2 \text { OR } 4.5 \end{aligned}$ | B1 <br> B1 <br> 11 | $\frac{\text { Must be } 18 \text { NOT } 21-\mathbf{3}}{(x=) 18 / 4 \text { gets } B 0 . \underline{(x=)} 9 / 2 \text { gets B0 }}$ |
| 9. (a) yuan $=700 \times 9.79$ $=6853 \text { (yuan) ISW }$ <br> 9. (b) $\begin{aligned} \text { Pounds } & =2447.5 / 9.79 \\ & =(£) 250 \quad \text { ISW } \end{aligned}$ | M1 <br> A1 <br> M1 <br> A1 <br> 4 | Yuan not required but A0 for $£ 6853$ <br> £ not required but A0 for 250 yuan |


| PAPER 2 (Calculator allowed) Foundation Tier | Marks | FINAL MARK SCHEME Comments |
| :---: | :---: | :---: |
| 10. (a) (10) 172431 <br> (b) (35 31) 272319 <br> (c) $\frac{(\text { Yes })}{6}$ because 100 is 60 away and 60 is divisible by <br> (d) After 5 steps 75 <br> (e) Starting numbers are 44 apart. <br> 44 is divisible by 4 | $\begin{aligned} & \text { B1 } \\ & \text { B1 } \\ & \text { E2 } \\ & \text { B1 } \\ & \text { B1 } \\ & \text { B1 } \\ & \text { B1 } \\ & 8 \\ & \hline \end{aligned}$ | E2 for $6 \times 10+40$ OR equivalent, e.g. Yes, in 10 steps (E2) <br> E1 for considering 60 with an indication of steps of 6 e.g. listing all numbers between 40 to 100 . <br> 75 can be answered in lists, but the 5 must be given as an answer. <br> Allow B1 for sight of 44 OR 40 by comparing 21 and 61 after one step etc. <br> SC 1 for only listing the correct sequences. |
| 11. (a) $(A \hat{C} B)=60\left({ }^{\circ}\right)$ $\begin{aligned} & (B \hat{C} E)=45\left(^{\circ}\right) \\ & (A \hat{C} E)=105\left(^{\circ}\right) \end{aligned}$ <br> 11. (a) (continued) <br> QWC <br> Look for <br> - Spelling <br> - Clarity of text explanations <br> - Some geometrical statements, e.g. angles of a equilateral triangle are $60^{\circ}$ <br> QWC2: Candidates will be expected to <br> - present work clearly, with words explaining their processes or steps <br> AND <br> - make few if any mistakes in mathematical form, spelling, punctuation and grammar and include units in their final answer <br> QWC1: Candidates will be expected to <br> - present work clearly, with words explaining their processes or steps <br> OR <br> - make few if any mistakes in mathematical form, spelling, punctuation and grammar and include units in their final answer | B1 <br> B1 <br> B1 <br> QWC <br> 2 | Look for the angles shown in their diagram (Angles of an equilateral triangle are $60^{\circ}$ ) <br> (Half the angle of a square is $45^{\circ}$ ) <br> C.A.O. <br> $105\left(^{\circ}\right)$ with NO supporting work gets 0. <br> QWC2 Presents relevant material in a coherent and logical manner, using acceptable mathematical form, and with few if any errors in spelling, punctuation and grammar. <br> QWC1 Presents relevant material in a coherent and logical manner but with some errors in use of mathematical form, spelling, punctuation or grammar. <br> OR <br> Evident weaknesses in organisation of material but using acceptable mathematical form, with few if any errors in spelling, punctuation and grammar. <br> QWC0 Evident weaknesses in organisation of material, and errors in use of mathematical form, spelling |
| 11. (b) First arcs <br> Final arcs and line <br> 11. (c) First arcs Final arcs and line | B1 <br> B1 <br> B1 <br> B1 <br> 9 | If no pair of compasses used (i.e no arcs) then 0 for their work in (b) and (c) <br> They can use the points $A$ and $B$ for this first B1 Remember the 2 methods discussed in the conference. |
| Use Overlay  <br> 12. Bearing from Holyhead <br> Bearing from Cardigan <br> Position of Ship | M1 <br> M1 <br> A1 $3$ | Use Overlay <br> Within $\pm 2^{\circ}$. Watch out for unambiguous 'dots' within <br> Within $\pm 2^{\circ}$ the boundaries of the overlay and award M1s <br> F.T. provided at least M1 <br> One unambiguous 'dot' within the 'box' on the overlay gets all 3 marks. |



PAPER 2-HIGHER TIER

| PAPER 2 <br> Higher Tier | Marks | FINAL MARK SCHEME Comments |
| :---: | :---: | :---: |
| $\text { 1. } \begin{aligned} \mathrm{a} & =76\left({ }^{\circ}\right) \\ \mathrm{b} & =53\left({ }^{\circ}\right) \\ \mathrm{c} & =51\left(^{\circ}\right) \end{aligned}$ | $\begin{gathered} \text { B1 } \\ \text { B1 } \\ \text { B1 } \\ 3 \end{gathered}$ | FT $180-(\mathrm{a}+\mathrm{b})$ |
| 2. (a) 23 (m) <br> (b) $(12+24) \div 4$ <br> 9 (car lengths) <br> (c) <br> (d) $15+0.30 \times 15 \quad$ OR $38+0.20 \times 38$ or equivalents 19.5 and 45.6 $65(.1 \mathrm{~m})$ | B1 <br> M1 <br> A1 <br> M1 <br> A2 <br> M1 <br> A2 <br> A1 $10$ | Evidence of a method, e.g. $\div 5$ and $\times 8$, or $\times 5$ and $\div 8$ as appropriate, or sight of a correct scale, e.g. $80 \times 30 / 50$ A1 for either answer correct. Also implies M1 <br> A1 for either correct answer. Accept 20 and 46 <br> FT from M1, A1 <br> FT from rounding to 'their $20^{\prime}+$ 'their 46 ' $=66(\mathrm{~m})$ Unsupported 65 or 66 gain full credit If no marks, SC 1 for an answer of 12.1 or 12 (giving the increase not the total) |
| 3.(a) Scale factor 2 enlargement (Intention of the) Correct position <br> (b) Correct rotation about $(2,1)$ | $\begin{gathered} \text { B1 } \\ \text { B1 } \\ \text { B2 } \\ 4 \end{gathered}$ | Perhaps watch for the position of the bottom left vertex B1 for rotation of $180^{\circ}$ about $(1,2)$ |
| ```4. Janie 450/1.57 or Ami 30000/129.82 Janie (£)286.6242\ldots or (£)286.62 Ami (£)231.0892.. or (£)231.08 or (£)231.09 or (£)231 (£)186.62 and 131.09``` | $\begin{aligned} & \text { M1 } \\ & \text { A1 } \\ & \text { A1 } \\ & \text { B1 } \end{aligned}$ | Allow (£)286.6(0) <br> Allow (£)231.1(0) <br> FT correctly subtracting (£) 100 from each of their amounts, but not from 450 or 30000 |
| Sight of an amount (not starting dollars or yen) $\times 1.18$ 669.9 (0 euros) or 669 (euros) or 670 (euros) | $\begin{gathered} \text { M1 } \\ \text { A1 } \end{gathered}$ | For method of conversion, even if $£ 250$ not added FT their (amounts in $£ s$ ) rounded or truncated, e.g. leading to 669.88 . Must be FT for the 3 girls e.g. $\{186$. (..) + |
| Look for <br> - spelling <br> - clarity of text explanations, <br> - the use of notation (watch for the use of ' $=$ ', $£$, \$, Yen being appropriate) | $\begin{gathered} \text { QWC } \\ 2 \end{gathered}$ | $131 .(\ldots)+250\} \times 1.18$ correctly evaluated, rounded or truncated <br> MR-1 for treat situation of exchange of money for whole notes |
| QWC2: Candidates will be expected to <br> - present work clearly, with words explaining process or steps <br> AND <br> - make few if any mistakes in mathematical form, spelling, punctuation and grammar and include units in their final answer |  | QWC2 Presents relevant material in a coherent and logical manner, using acceptable mathematical form, and with few if any errors in spelling, punctuation and grammar. <br> QWC1 Presents relevant material in a coherent and logical manner but with some errors in use of mathematical form, spelling, punctuation or grammar OR |
| QWC1: Candidates will be expected to <br> - present work clearly, with words explaining process or steps <br> OR <br> - make few if any mistakes in mathematical form, spelling, punctuation and grammar and include units in their final answer | 8 | evident weaknesses in organisation of material but using acceptable mathematical form, with few if any errors in spelling, punctuation and grammar. <br> QWC0 Evident weaknesses in organisation of material, and errors in use of mathematical form, spelling, punctuation or grammar. |

\begin{tabular}{|c|c|c|}
\hline PAPER 2 Higher Tier \& Marks \& FINAL MARK SCHEME \\
\hline \begin{tabular}{l}
5.(a) 7.6 (cm) \\
(b)(i) Mid-points 5,6,7,8,9
\[
5 \times 4+6 \times 2+7 \times 1+8 \times 1+9 \times 2
\] \\
Intention their \(\sum \mathrm{fx} / 10\) \(6.5(\mathrm{~cm})\) \\
(ii) Modal class \(4.5 \leq \mathrm{s}<5.5\) Median \(\quad 5.5 \leq \mathrm{s}<6.5\)
\end{tabular} \& \[
\begin{gathered}
\hline \text { B1 } \\
\text { B1 } \\
\text { M1 } \\
\\
\text { m1 } \\
\text { A1 } \\
\text { B1 } \\
\text { B1 } \\
7 \\
\hline
\end{gathered}
\] \& \begin{tabular}{l}
FT their mid points including bounds provided they fall within the classes. \(20+12+7+8+18(=65)\) \\
(65/10) For correct evaluation of \(\sum \mathrm{fx} / 10\) \\
Accept '4.5 to 5.5 ' \\
Accept ' 5.5 to 6.5 '
\end{tabular} \\
\hline \begin{tabular}{l}
6.(a) Radius 2.3 \\
\(\Pi \times 2.3^{2} \times 8.4\) \\
\(139.5\left(998 \ldots \mathrm{~cm}^{3}\right)\) to \(139.7\left(\mathrm{~cm}^{3}\right)\) \\
(b)(i)
\[
\begin{aligned}
\& \left(x^{2}=\right) 3.4^{2}+5.6^{2} \\
\& x^{2}=42.92 \text { or } x=\sqrt{ } 42.92 \\
\& 6.6(\mathrm{~cm})
\end{aligned}
\] \\
(ii) \(1 / 2 \times 5.6 \times 3.4\)
\[
9.5\left(2 \mathrm{~cm}^{2}\right)
\]
\end{tabular} \& \begin{tabular}{l}
B1 \\
M1 \\
A1 \\
M1 \\
A1 \\
A2 \\
M1 \\
A1 \\
9
\end{tabular} \& \begin{tabular}{l}
Do not accept from premature approximate SC1 for an answers \(558\left(.3992 \ldots \mathrm{~cm}^{3}\right)\) to \(558.7\left(\mathrm{~cm}^{3}\right)\) \\
Depends on previous M1 and process of \(\sqrt{ }\). Mark final answer. \\
A1 for \(6.5(51 \ldots \mathrm{~cm})\) \\
Mark final answer
\end{tabular} \\
\hline \begin{tabular}{l}
7.(a) Correct frequency polygon \\
(b) \(226090 \quad 100\) \\
(c) Uniform scale vertically Plotting all points at the upper bounds
\end{tabular} \& \begin{tabular}{l}
\[
\overline{\mathrm{B} 2}
\] \\
B1 \\
B1 \\
B2
\end{tabular} \& \begin{tabular}{l}
Must be accurate between bounds of 1 small square horizontally and on the line vertically \\
B1 if translated OR joined with curve or not joined OR one plot incorrect within the polygon \\
Ignore frequency diagram as working \\
Appropriate for their values in (b) \\
FT their cumulative table only if cumulative \\
Ignore if (50, 0) omitted \\
Must be accurate on vertical lines and horizontal lines B1 if one error in plots, OR for all vertical plots correct but not at upper bounds
\end{tabular} \\
\hline \begin{tabular}{l}
All 6 accurate upper bound plots joined with a curve or lines \\
(d)(i) Median for their graph \\
(ii) Idea UQ - LQ, with an attempt at readings and intention to subtract Interquartile range accurate for their graph
\end{tabular} \& B1
B1
M1
A1
10
1 \& \begin{tabular}{l}
FT from their cumulative graph in (d)(i) and (ii) (Answer in the range 63.5 to \(64(\mathrm{~cm})\) )
\[
\text { ( } 67 \text { to } 68-60 \text { to } 60.5 \text { ) }
\] \\
(Answers in the range 6.5 to 7.5 )
\end{tabular} \\
\hline \begin{tabular}{l}
8.(a)(i) \\
(ii) \(161296\left(.875 \mathrm{~cm}^{3}\right)\) or \(161297\left(\mathrm{~cm}^{3}\right) \quad\) ISW \\
(b) Least: \((x-0.5)(y-0.5)(z-0.5)\)
\end{tabular} \& B2
B2

B2

6 \& | B1 for any 3 correct entries |
| :--- |
| Accept $.49^{\circ}$ RECURRING as being equivalent to .5 |
| FT their greatest provided all > given values and <47, <56 and <63 respectively |
| B1 for selection of $46.5(\times) 55.5(\times) 62.5$ (sight of digits 161296 or 161297). Allow SC1 for an answer of 164.5 , or for selecting and recording addition for their greatest values B1 for minor slip, or omission of brackets, there needs to be intention to multiply, or if further incorrect working B0 for sight of the 3 terms only without intention to multiply | <br>

\hline | 9. $\quad \tan \mathrm{A}=3.2 / 7$ |
| :--- |
| $24.567 \ldots\left({ }^{\circ}\right)$ rounded or truncated | \& \[

$$
\begin{gathered}
\hline \text { M1 } \\
\text { A2 } \\
3 \\
\hline
\end{gathered}
$$

\] \& | A1 for $0.457 \ldots$ or $\tan ^{-1} 3.2 / 7$ |
| :--- |
| SC1 for calculating B, an answer of $65.43 \ldots\left({ }^{9}\right)$, this is not for an answer labelled as A | <br>

\hline
\end{tabular}

| PAPER 2 <br> Higher Tier | Marks | FINAL MARK SCHEME Comments |
| :---: | :---: | :---: |
| 10.(a) Method, equating coefficients or alternative First variable correct Method to find second variable Second variable correct <br> (b) $\begin{aligned} & 11(3+x)+2(2 x-1)=13 \times 2 \times 11 \\ & 15 x+31=286 \\ & x=17 \end{aligned}$ <br> (c) $\begin{aligned} 7 r-a r & =b-c \\ r(7-a) & =b-c \\ r & =(b-c) /(7-a) \quad \text { or equivalent } \end{aligned}$ | $\begin{aligned} & \text { M1 } \\ & \text { A1 } \\ & \text { M1 } \\ & \text { A1 } \\ & \text { M2 } \\ & \text { A1 } \\ & \text { A1 } \\ & \text { B1 } \\ & \text { B1 } \\ & \text { B1 } \\ & 11 \end{aligned}$ | Allow 1 slip, but not in equated coeffs. $x=11 y=-3$ <br> FT their first variable <br> No M mark if left as quotient <br> M1 for 2 of these 3 terms correct <br> FT from M1 for A1 only <br> CAO (Must be simplified) <br> Like terms FT until second error <br> Factorise <br> Isolate |
| 11.(a) 0.05 <br> (b) $1.1 \times 10^{-4}$ | $\begin{gathered} \text { B1 } \\ \text { B2 } \\ \\ 3 \\ \hline \end{gathered}$ | Accept equivalents, $1 / 20$ <br> B1 for $1 \times 10^{-4}$ or $1.11 \times 10^{-4}$ or $1.111 \ldots \times 10^{-4}$ SC1 FT from their (a)/450 correctly expressed in standard form |
| 12.(a) $(\mathrm{y}=) 360-2 \mathrm{x}$ or $\quad(\mathrm{y}=) 2(180-\mathrm{x}) \quad$ ISW <br> (b) FGH $=90^{\circ}$ seen or implied by used in calculation $\begin{aligned} & \mathrm{FH}=6.8 / \sin 32(\times \sin \mathrm{FGH}) \\ & \mathrm{FH}=12.8(32 . . \mathrm{cm}) \text { or } 13(\mathrm{~cm}) \end{aligned}$ | $\begin{gathered} \hline \text { B2 } \\ \\ \text { B1 } \\ \text { M2 } \\ \text { A1 } \\ 6 \end{gathered}$ | B1 for appropriate 2 x , or $180-\mathrm{x}$ may be seen on the diagram or labelled, OR B1 for $x=(360-y) / 2$, or a correct expression but not ' $y=.$. ' <br> M 1 for $\sin 32=6.8 / \mathrm{FH}$ or $\mathrm{FH} / \operatorname{sinFGH}=6.8 / \sin 32$ Answer of 12 gets A0 |
| 13. | $\begin{gathered} \text { B1 } \\ \text { B1 } \\ 2 \\ \hline \end{gathered}$ | Accept descriptions <br> Do not accept e.g. 'dashes in the same places' Must be clear that it is the included angle |
| 14. Strategy to find ( $1 / 2$ ) PQ and $<\mathrm{PBQ}$ $\mathrm{PQ}^{2}=4^{2}+6^{2}-2 \cdot 4 \cdot 6 \cdot \operatorname{Cos} 82$ $\mathrm{PQ}^{2}=45.31969 \ldots$ <br> $\mathrm{PQ}=6.73199 \ldots$. $\mathrm{PQ}^{2}=8^{2}+8^{2}-2 \cdot 8 \cdot 8 \cdot \operatorname{Cos} \mathrm{PBQ}$ $\begin{aligned} \operatorname{Cos} \mathrm{PBQ}= & \frac{8^{2}+8^{2}-\mathrm{PQ}^{2}}{2.8 .8} \\ & <\mathrm{PBQ}=49.763 \ldots\left({ }^{\circ}\right) \end{aligned}$ $\begin{aligned} \text { Area shaded } & =(<\mathrm{PBQ} / 360) \times \Pi \times 8^{2} \\ & =27.79 . .\left(\mathrm{cm}^{2}\right) \text { or } 28\left(\mathrm{~cm}^{2}\right) \text { or } 27.8\left(\mathrm{~cm}^{2}\right) \end{aligned}$ | S1 M1 A1 A1 M1 A1 A1 M1 A1 9 | Maybe embedded <br> OR Alternative: $\begin{array}{rlrl} \sin 1 / 2 P B Q & =1 / 2 P Q / 8 & & M 1 \\ <1 / 2 P B Q & =24.88 \ldots & & A 1 \\ <P B Q & =49.763 \ldots\left({ }^{\circ}\right) & A 1 \end{array}$ <br> Accept answers in the range 49.5 to 49.8 inclusive, or 50 Correct answer, not FT <br> FT their $<\mathrm{PBQ}$ provided not 82 and all M marks awarded Accept answers in the range 27.6 to 28 inclusive |
| 15.(a) Decision to find overall totals of a, e, $r$ and number of letters $34 / 132$ or $0.2575 \ldots$ or equivalent <br> (b)Use or sight of (a, e, r =) 34 AND (number of letters =) 132 , OR, sight of any correct probability product, equivalent to .. $/ 132 \times . . / 131$ (or .../66×.../65) as appropriate <br> $\mathrm{P}($ at least one of $\mathrm{a}, \mathrm{e}, \mathrm{r})=1-\mathrm{P}($ none $)$ <br> OR equivalent full strategy <br> $1-98 / 132 \times 97 / 131$ or equivalent full method $0.45$ | $\begin{gathered} \hline \text { M1 } \\ \text { A1 } \\ \text { B1 } \\ \text { S1 } \\ \text { M1 } \\ \text { A2 } \\ 7 \end{gathered}$ | (34 and 132) <br> Mark final answer <br> Accept sight of 34 and 132, or 17 and 66. FT from (a) For the idea without need to use values <br> (As $66=132 \div 2$ ) <br> FT their totals, a method that would lead to correct answer A1 for answer not correct to 2dp, as a result of incorrect or premature rounding <br> N.B. Markers check working for no replacement |
| 16. Cosine curve from $0^{\circ}$ to $360^{\circ}$ <br> Correct cosine curve with the correct translation, with 2 marked on the $y$-axis | $\begin{gathered} \mathrm{M} 1 \\ \text { A1 } \\ 2 \\ \hline \end{gathered}$ | Any vertical translation, but must be correct horizontally Accept if numbers of degrees missed but unambiguous |

WJEC
245 Western Avenue
Cardiff CF5 2YX
Tel No 02920265000
Fax 02920575994
E-mail: exams@wjec.co.uk website: www.wjec.co.uk

