## MARKING SCHEMES

## MATHEMATICS PILOT SCHEME

WJJEC

## INTRODUCTION

The marking schemes which follow were those used by the WJEC for the 2006 examination in GCSE Mathematics Pilot Scheme. They were finalised after detailed discussion at examiners' conferences by all the examiners involved in the assessment. The conferences were held shortly after the papers were taken so that reference could be made to the full range of candidates' responses, with photocopied scripts forming the basis of discussion. The aim of the conferences was to ensure that the marking schemes were interpreted and applied in the same way by all examiners.

It is hoped that this information will be of assistance to centres but it is recognised at the same time that, without the benefit of participation in the examiners' conferences, teachers may have different views on certain matters of detail or interpretation.

The WJEC regrets that it cannot enter into any discussion or correspondence about these marking schemes.

| GCSE Pilot 2006 <br> Mathematics Foundation Tier Paper 1 | Mark | Final Mark Scheme Comments |
| :---: | :---: | :---: |
| 1. (a) $12 \quad 22 \quad 102122 \quad 202 \quad 212 \quad 221$ <br> (b) (i) 111 <br> (ii) 34 <br> (iii) 72 <br> (iv) 8 <br> (c) (£) $115,750(\cdot 00)$ | $\begin{gathered} \text { B1 } \\ \text { B1 } \\ \text { B1 } \\ \text { B1 } \\ \text { B1 } \\ \text { B1 } \\ 6 \end{gathered}$ | $\begin{aligned} & \mathrm{CAO} \\ & \mathrm{CAO} \\ & \mathrm{CAO} \\ & \mathrm{CAO} \\ & \mathrm{CAO} \\ & \mathrm{CAO} \end{aligned}$ |
| 2. (a) 4 correct lines <br> (b) Complete figure | $\begin{gathered} \text { B2 } \\ \text { B2 } \\ 4 \end{gathered}$ | ```B1 for 2 correct lines only. B1 for 4 correct lines + additional line(s) -1 for each incorrect vertex, max. -2``` |
| 3. (a) Friday <br> (b) 19 <br> (c) Tuesday and Wednesday <br> (d) $20,14,6,19,23$, 82 | B1 <br> B1 <br> B1 <br> M1 <br> A1 <br> 5 | CAO <br> CAO <br> CAO <br> Attempt to add at least 4 of the numbers <br> FT for $63+$ 'their (b)' |
| 4. (a) <br> (i) 24 <br> (ii) 11 <br> (b) (i) $4 \times 8+45$ <br> (£) 77 <br> (ii) $\begin{aligned} 8 \mathrm{~N} & =61-45 \\ \mathrm{~N} & =(2 \text { hours }) \end{aligned}$ | $\begin{gathered} \hline \text { B1 } \\ \text { B1 } \\ \\ \text { M1 } \\ \text { A1 } \\ \text { M1 } \\ \text { A1 } \\ 6 \end{gathered}$ | $\begin{aligned} & \text { CAO } \\ & \text { CAO } \end{aligned}$ <br> Must attempt to multiply and add CAO CAO |
| 5. (a) (i) 49  <br>   (ii) 17 <br> (ii) 17 <br> (iii) 32 <br> (b) $20 \times 60 / 100$ OR $10 \%=(£) 6$ <br> (£) 12 ISW $20 \%=(£) 12$ <br> (c) (i) (0) $\cdot 75$ <br> (0) $\cdot 6(0)$ <br> (i) $60 \% 0.7 \frac{3}{4}$ | $\begin{gathered} \text { B1 } \\ \text { B1 } \\ \text { B1 } \\ \\ \text { M1 } \\ \text { A1 } \\ \\ \text { B1 } \\ \text { B1 } \\ \text { B1 } \\ 8 \end{gathered}$ | CAO <br> CAO <br> CAO <br> CAO <br> FT from (i) |
| 6. $\quad 120125125125130130134145155$ <br> Median (£) 130 <br> Range (f) 35 | $\begin{gathered} \text { M1 } \\ \text { B1 } \\ \text { A1 } \\ \text { B1 } \\ 4 \end{gathered}$ | $\begin{aligned} & \mathrm{CAO} \\ & \mathrm{CAO} \\ & \mathrm{CAO} \end{aligned}$ |
| $\text { 7. } \begin{array}{ll} \text { Angle } \mathrm{CAB}=57^{\circ} \\ \text { Angle } \mathrm{ACB}=63^{\circ} \\ & \mathrm{AB}=11.6 \mathrm{~cm} \end{array}$ | $\begin{gathered} \text { B1 } \\ \text { B1 } \\ \\ \text { B1 } \\ 3 \end{gathered}$ | $\pm 2^{\circ} \quad$ Give B1 if both angles are correct $\pm 2^{\circ} \quad$ but reversed. $\pm 2 \mathrm{~mm}$ FT from their diagram |


| GCSE Pilot 2006 <br> Mathematics Foundation Tier <br> Paper 1 |  | Mark |
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| GCSE Pilot 2006 <br> Mathematics Foundation Tier Paper 1 | Mark | Final Mark Scheme Comments |
| :---: | :---: | :---: |
| 12. (a) -1 <br> (b) Plot 2 correct points OR 3 correct points taken from their table Draw line | B1 <br> B1 <br> B1 <br> 3 | CAO CAO |
| 13. (a) All points plotted correctly <br> (b) Negative | B1 B1 $3$ | B1 for at least 3 correct plots, B1 for 5 correct points joined by lines B1 if tests reversed. Ignore line of best fit. <br> Do not accept descriptions. |
| 14. (a) $\begin{aligned} & 20 \times 15 \times 10 \\ & \\ & 3000\left(\mathrm{~cm}^{3}\right)\end{aligned}$ <br> (b) $3000 / 100$ <br> $30(\mathrm{~cm})$ | $\begin{gathered} \text { M1 } \\ \text { A1 } \\ \\ \text { M1 } \\ \text { A1 } \\ 4 \\ \hline \end{gathered}$ | CAO <br> FT from (a) |
| 15. $\begin{aligned} & 1 / 2 \times 5 \times 6 \\ & 15 \\ & \\ & \mathrm{~cm}^{2}\end{aligned}$ | $\begin{gathered} \text { M1 } \\ \text { A1 } \\ \text { U1 } \\ 3 \end{gathered}$ | Attempt $1 / 2$ base x height seen e.g. $2 \cdot 5 \times 6$ |
| 16. (a) $20 \times 200 / 100$ <br> (£) 240 <br> (b) (i) $100 / 5$ <br> Nigel (£)80 Paul (3)20 <br> (ii) No <br> 4:1, OR 36, 9 matches OR Nigel 4, Paul 1, then repeat etc OR NNNNPNNNNP .... OR | $\begin{gathered} \text { M1 } \\ \text { A1 } \\ \text { A1 } \\ \\ \text { M1 } \\ \text { A1 } \\ \text { B1 } \\ \text { E1 } \\ 7 \end{gathered}$ | M1 A1 for $1 \cdot 2 \times 200$ <br> FT <br> Accept Nigel ( $\mathfrak{f}$ )20 Paul ( $\mathfrak{f}$ ) 80 for M1 CAO <br> May be implied in the explanation. <br> FT their (b)(i) logic. <br> 'Nigel should go more' is insufficient. |
| 17. (a) Method that produces at least 2 correct prime factors. <br> Sight of correct factors. <br> (2,2,2,3,3,5) <br> $2^{3} \times 3^{2} \times 5$ or $2^{3} .23^{2} .5$ <br> (b) e.g. odd powers, index 5 is not even, etc. | M1 <br> A1 <br> B1 <br> E1 <br> 4 | Ignore 1s seen <br> FT their factors (with at least one index $>1$ used). Do not ignore 1s |
| 18. (a) Bisector of angle CAB <br> Arc centre B radius 6 cm Shaded area <br> (b) Enlargement $1 / 2$ Correct position | B1 B1 B1 B1 B1 5 | $\begin{aligned} & \pm 2^{\circ} \\ & \pm 2 \mathrm{~mm} \\ & \text { FT for the intention of bisector and arc. } \end{aligned}$ |
| 19. $\begin{array}{lll}0 \cdot 12+0 \cdot 34 \\ & 0.46 & 46 / 100\end{array} \quad 46 \%$ | $\begin{gathered} \text { M1 } \\ \text { A1 } \\ 2 \\ \hline \end{gathered}$ |  |

\begin{tabular}{|c|c|c|}
\hline \begin{tabular}{l}
GCSE Pilot 2006 \\
Mathematics Foundation Tier Paper 2
\end{tabular} \& Mark \& Final Mark Scheme Comments \\
\hline \begin{tabular}{l}
1. \\
(b) \(40 \div 2.56\)
\end{tabular} \& B1
B1
B1
B1
M1
A1
6 \& \begin{tabular}{l}
CAO \\
CAO \\
CAO \\
FT for one error \\
CAO Answer only 15.6(25) M1 A0
\end{tabular} \\
\hline \begin{tabular}{l}
2. (a) Pentagon \\
Hexagon Parallelogram Trapezium \\
(b) Diameter Tangent Chord
\end{tabular} \& \[
\begin{gathered}
\hline \text { B1 } \\
\text { B1 } \\
\text { B1 } \\
\text { B1 } \\
\text { B1 } \\
\text { B1 } \\
\text { B1 } \\
7
\end{gathered}
\] \& Accept names written at the side of the diagrams. Accept a list written in order if completely correct. \\
\hline \begin{tabular}{l}
3. (a) \(\begin{aligned} \& \mathrm{F} \\ \& \mathrm{H}\end{aligned}\) \\
(b) \(\mathrm{P} \quad \mathrm{S}\)
\end{tabular} \& \[
\begin{gathered}
\text { B1 } \\
\text { B1 } \\
\\
\text { B1 } \\
3
\end{gathered}
\] \& \begin{tabular}{ll} 
CAO \& B1 for diagrams \(F\) and \(H\) clearly \\
CAO \& \begin{tabular}{l} 
marked, with no other diagram \\
marked.
\end{tabular} \\
CAO
\end{tabular} \\
\hline \begin{tabular}{l}
4. (a) Seven thousand(s) nine hundred and four \\
(b) (i) Shade any four squares \\
(ii) \(7 / 16\) ISW \\
(c) \(\quad 8753\)
\end{tabular} \& \begin{tabular}{l}
B1 \\
B1 \\
B1 \\
B1 \\
B 1
5
\end{tabular} \& \begin{tabular}{l}
Words only. \\
BO for seven thousandths etc. \\
CAO B1 for seven sixteenths B0 for seven out of sixteen \\
CAO \\
CAO
\end{tabular} \\
\hline \begin{tabular}{l}
5. Five days correct \\
\(\left.\begin{array}{lllll}(2 \& 3 \& 11 / 2 \& 21 / 4 \& 13 / 4 \\ \text { symbols }\end{array}\right)\)
\end{tabular} \& B4

4 \& | -1 once only for use of a different symbol |
| :--- |
| B3 Four days correct |
| B2 Three days correct |
| B1 Two days correct | <br>

\hline | 6. (a) Draw pattern OR $8+10+12$ |
| :--- |
| (b) $\quad \begin{aligned} & (3+8) \times 6 \\ & 66\end{aligned}$ |
| (c) (i) $\operatorname{Plot} \mathrm{P}(-3,-5)$ |
| Plot Q $(-4,3)$ |
| (ii) $\mathrm{D}(2,4)$ | \& \[

$$
\begin{gathered}
\text { M1 } \\
\text { A1 } \\
\\
\text { M1 } \\
\text { A1 } \\
\\
\text { B1 } \\
\text { B1 } \\
\text { B1 } \\
7 \\
\hline
\end{gathered}
$$

\] \& | One error allowed for M1 |
| :--- |
| CAO. Answer 6 more gets M1 A0. |
| CAO |
| P and Q need not be shown on the diagram. |
| CAO |
| No marks awarded when the coordinates are reversed. | <br>

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\end{tabular}

| GCSE Pilot 2006 Mathematics Foundation Tier Paper 2 | Mark | Final Mark Scheme Comments |
| :---: | :---: | :---: |
| 7. (a) A at or very near 1 B at or near $1 / 6$ C at or very near 0 <br> (b) $\begin{aligned} & 56+54+\ldots . .+85 \\ & \text { 'their total' } \div 12 \\ & 69 \end{aligned}$ (828) | $\begin{gathered} \text { B1 } \\ \text { B1 } \\ \text { B1 } \\ \\ \text { M1 } \\ \text { m1 } \\ \text { A1 } \\ 6 \end{gathered}$ | $>0,<1 / 4$ CAO |
| 8. $\begin{aligned} & 101.25 \\ & 149.40-101.25 \\ & \text { (£) } 48.15 \\ & 48.15 \div 9 \\ & \text { (£) } 5.35 \end{aligned}$ <br> (b) $\frac{12 \times 650}{100}$ <br> (£)78 (ISW) | $\begin{gathered} \text { B1 } \\ \text { M1 } \\ \text { A1 } \\ \text { m1 } \\ \text { A1 } \\ \text { M1 } \\ \\ \text { A1 } \\ 7 \end{gathered}$ | CAO FT FT Answer only (£)572 OR (£)728 gets M1 A0 CAO <br> Answer only (£)572 OR (£)728 gets M1 A0 CAO |
| 9. (a) $\begin{aligned} & 14 \text { books } \\ & 2 \text { left }\end{aligned}$ <br> (b) (i) 1.9 <br> (ii) 1.5625 or 1.563 or 1.56 <br> (iii) 16 OR 27 <br> 432 <br> (iv) 4.76 <br> (c) $\begin{aligned} & 2 / 5 \text { of } 500=200 \\ & 1 / 4 \text { of } 500=125 \\ & \text { amount left }=500-325=175 \\ & \text { Fraction left }=175 / 500 \mathrm{ISW}(1 / 20) \end{aligned}$ <br> OR $\begin{aligned} & 8 / 20+5 / 20 \\ & 13 / 20 \end{aligned}$ <br> Fraction left $1-13 / 20$ ${ }^{7} / 20$ ISW | B1 <br> B1 <br> B1 <br> B2 <br> B1 <br> B1 <br> B1 <br> B1 <br> B1 <br> M1 <br> A1 <br> B1 <br> B1 <br> M1 <br> A1 12 | CAO <br> CAO <br> CAO <br> B1 for sight of 0.64 . $B 0$ for answer only 1.6 |
| 10. (a) (i) Labels on axes Correct line <br> (ii) 43.2 or reading from 'their line' <br> (b) (i) 45 (miles) <br> (ii) 75 (minutes) 1 h 15 m <br> (iii) 20 (miles) | $\begin{gathered} \hline \text { B1 } \\ \text { M1 } \\ \text { A1 } \\ \text { B1 } \\ \\ \text { B1 } \\ \text { B1 } \\ \text { B1 } \\ 7 \\ \hline \end{gathered}$ | CAO <br> Accept 44 or 46(miles) <br> BO for 1.15(h) |


| GCSE Pilot 2006 Mathematics Foundation Tier Paper 2 | Mark | Final Mark Scheme Comments |
| :---: | :---: | :---: |
| 11. (a) (i) $057^{\circ}$ <br> (ii) Actual length $=20 \times 8(\mathrm{~m})$ 156 (m) to 164 (m) <br> (b) Line from A on correct bearing $\pm 2^{\circ}$ Line from $B$ on correct bearing $\pm 2^{\circ}$ Lines intersect at $P$ | B1 <br> M1 <br> A1 <br> M1 <br> M1 <br> A1 <br> 6 | $\pm 2^{\circ} \quad 57^{\circ}$ is B0 <br> M1 for $20 \times$ 'their length' <br> Allow $\pm 2 \mathrm{~mm}$ in length of TB <br> One line correct one incorrect and the two lines intersecting gets M0 M1 A1 <br> One point in the correct region gets M1 M1 A1 |
| 12. (a) $450 \times 9.8$ <br> (b) $627.2 \div 9.8$ <br> (£) 64 | $\begin{gathered} \text { M1 } \\ \text { A1 } \\ \\ \text { M1 } \\ \text { A1 } \\ 4 \end{gathered}$ | $\begin{aligned} & \mathrm{CAO} \\ & \mathrm{CAO} \end{aligned}$ |
| 13. $\begin{aligned} & x=48^{\circ} \\ & y=37^{\circ} \end{aligned}$ <br> (b) Exterior angle $=360 / 8$ $\text { Interior angle }=135^{\circ}$ | $\begin{gathered} \hline \mathrm{B} 1 \\ \mathrm{~B} 1 \\ \\ \mathrm{M} 1 \\ \\ \mathrm{~A} 1 \\ 4 \end{gathered}$ | CAO <br> CAO <br> M1 for any correct method. $(2 \times 8-4) \times 90 / 8, \quad 1080 / 8$ CAO |
| 14. (a) $\begin{aligned} & 2 x+5+2 x+5+3 x+3 x \\ & 10 x+10 \text { ISW }\end{aligned}$ <br> (b) $\begin{aligned} & 8 x+4 x=7-4 \\ & 12 x=3 \\ & x=3 / 12 \text { ISW } \quad(1 / 4 \quad 0.25) \end{aligned}$ <br> (c) $\begin{array}{lc} 10 x-15=50 & \text { or } 2 x-3=50 / 5 \\ 10 x=65 & 2 x=13 \\ x=65 / 10 & x=13 / 2 \\ \text { ISW } & \text { ISW } \\ (6.5) & (6.5) \end{array}$ <br> (d) $2 \times(x-3)$ | M1 <br> A1 <br> B1 <br> B1 <br> B1 <br> B1 <br> B1 <br> B1 <br> B2 <br> 10 | CAO <br> Stop at second error <br> FT <br> FT <br> Accept embedded answers for (b) and (c) <br> Stop at second error <br> FT <br> FT <br> B1 for partial factorisation $2\left(x^{2}-3 x\right) \text { or } x(2 x-6) \text { or } 2 x(x \ldots) \text { or } 2 x(\ldots-3)$ |
| ```15. \(\quad \mathrm{TR}^{2}=6.3^{2}-3.7^{2}\) \(\mathrm{TR}^{2}=26\) \(\mathrm{TR}=5.1\) or \(5(\mathrm{~cm})\) OR \(\cos \mathrm{S}=3.7 / 6.3 \quad \sin \mathrm{~T}=3.7 / 6.3\) and \(\quad \mathrm{TR}=6.3 \operatorname{sinS} \quad \mathrm{TR}=3.7 \tan \mathrm{~S} \quad \mathrm{TR}=3.7 / \tan \mathrm{T}\) \(\mathrm{TR}=5.1 \ldots\). \(\mathrm{TR}=5.1\) or \(5(\mathrm{~cm})\)``` | $\begin{gathered} \text { M1 } \\ \text { A1 } \\ \text { A1 } \\ \\ \text { M1 } \\ \text { A1 } \\ \text { A1 } \\ 3 \end{gathered}$ | Give M1 for $\mathrm{TR}^{2}+3.7^{2}=6.3^{2}$ <br> CAO <br> FT <br> Complete method for finding TR must be seen. |


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| 16. Mid points $154,161,168$ $\begin{aligned} & 154 \times 18+161 \times 37+168 \times 25 \\ & 12929 \\ & 161.6(125) \end{aligned}$ | B1 <br> M1 <br> A1 <br> A1 <br> 4 | FT for their mid points from within groups (not bounds). <br> FT for correct sum of their $f x$ terms. <br> FT for their $\Sigma f x / 80$ correctly evaluated. <br> Do not allow 161. <br> Unsupported 161.6125 awarded all 4 marks. <br> SC1 for bounds with correct FT answer (lower <br> 158.6125 upper 164.6125). |
| 17. (a) $1 / 2 \times \pi \times 6.4^{2}$ <br> 64.(33....cm ${ }^{2}$ ) <br> (b) Area $\times$ length $=2.5 \times 1.6 \times(100)$ Change of units e.g. 160 or $\times 100$ shown $400\left(\mathrm{~cm}^{3}\right)$ | M1 <br> A1 <br> M1 <br> M1 <br> A1 <br> 5 | SC1 for 128.(...), 257.(...) <br> Change of units not necessarily shown <br> CAO |


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| :---: | :---: | :---: |
| 1. (a) All points plotted correctly <br> (b) Negative | B2 B1 $3$ | B1 for at least 3 correct plots, or B1 if tests reversed Ignore line of best fit, Penalise joined point to point -1 <br> Do not accept descriptions. |
| 2. $\begin{aligned} & 3 \mathrm{a}+6 \mathrm{~b}+\ldots . . \\ & 10 \mathrm{a} \\ & \\ & -2 \mathrm{~b}\end{aligned}$ | $\begin{gathered} \text { B1 } \\ \text { B1 } \\ \text { B1 } \\ 3 \\ \hline \end{gathered}$ | Expansion of brackets FT for their expansion FT for their expansion |
| 3. (a) $x=2$ (cm) and $\mathrm{y}=5$ (cm) <br> (b) $11+8+4+x+y+7+2+3$ <br> $=42(\mathrm{~cm})$ <br> (c) $8 \times 4+5 \times 10+2 \times 3$ or $3 \times 11+7 \times 9-$ $4 \times 2$ or equivalent <br> $88\left(\mathrm{~cm}^{2}\right)$ | B2 <br> M1 <br> A1 <br> M2 <br> A1 <br> 7 | B1 for one correct or methods for finding both shown FT their x and y values from (a), $35+x+\mathrm{y}$ for $\mathrm{M} \& \mathrm{~A}$ marks <br> FT their x \& y for M marks only. M1 for attempt showing total area with 1 area correct CAO |
| 4. (a) $\mathrm{a}=70^{\circ}, \mathrm{b}=70^{\circ}, \mathrm{c}=110^{\circ}, \mathrm{d}=35^{\circ}$ <br> (b) (i) Bearing $329^{\circ} \pm 2^{\circ}$ <br> (ii) $036^{\circ} \pm 2^{\circ}$ from D $285^{\circ} \pm 2^{\circ}$ from E <br> G indicated or implied by point | $\begin{gathered} \text { B4 } \\ \text { B1 } \\ \text { M1 } \\ \text { M1 } \\ \text { A1 } \\ 88 \end{gathered}$ | B1 for each, FT from previous answers when logical <br> Depends on at least 1 M mark |
| 5. $\begin{aligned} & 1 / 2 \times 5 \times 6 \\ & =15\left(\mathrm{~cm}^{2}\right) \end{aligned}$ | $\begin{gathered} \text { M1 } \\ \text { A1 } \\ 2 \end{gathered}$ | Attempt $1 / 2$ base $\times$ height seen, e.g. $2.5 \times 6$ |
| 6. (a) Correct reflection in the line $\mathrm{y}=-1$ <br> (b) Correct translation | $\begin{gathered} \text { B2 } \\ \text { B1 } \\ 3 \\ \hline \end{gathered}$ | B1 for a reflection in any line indicated, or B1 for drawing $\mathrm{y}=-1$ |
| $\begin{array}{lll}\text { 7. (a) } & 50 \\ & 50 / 200(\times 100) \\ & 25 \%\end{array}$ <br> (b) (i) $100 / 5$ <br> Nigel (£)80 and Paul (£)20 <br> (ii) No <br> 1/5, 4/5 OR 9, 36 matches OR Nigel 4, Paul 1, then repeat etc. OR NNNNPNNNNP...OR .. | M1 <br> M1 <br> A1 <br> M1 <br> A1 <br> B1 <br> E1 <br> 7 | SC1 for 125\%..Penalise -1 for further working after $25 \%$. <br> CAO <br> Maybe implied in explanation <br> FT their (b)(i) logic. <br> "Nigel should go more" is insufficient. |


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| 8. (a) 2,11 <br> (b) Plots correct, allowing one error All points correct \& joined with a curve | B2 <br> B1 <br> B1 <br> 4 | B1 for each <br> FT from (a) <br> FT from (a) |
| 9. (a) Method that produces at least 2 correct prime factors Sight of correct factors (2, 2, 2, 3, 3, 5) $2^{3} \times 3^{2} \times 5$ or $2^{3} .3^{2} \cdot 5$ <br> (c) E.g. Odd power, index 5 is not even, ... | M1 <br> A1 <br> B1 <br> E1 <br> 4 | Ignore 1s seen <br> FT their factors (with at least on index $>1$ used). Do not ignore 1s. |
| 10. (a) Bisector of angle CAB Arc radius 6 cm centre $B$ Correct region shaded <br> (b) Enlargement $1 / 2$ Correct position | $\begin{gathered} \text { B1 } \\ \text { B1 } \\ \text { B1 } \\ \\ \text { B1 } \\ \text { B1 } \\ 5 \end{gathered}$ | $\begin{aligned} & \pm 2^{\circ} \\ & \pm 1 \mathrm{~mm} \\ & \text { FT for intention of bisector \& arc } \end{aligned}$ |
| 11. Correct frequency polygon | B2 $2$ | IGNORE bars if polygon drawn. <br> B1 for 4 correct plots, or correct vertical plots, or correct horizontal plots. SC1 for correct frequency diagram or SC 1 for translated polygon. |
| $\text { 12. } \begin{aligned} & 0.12+0.34 \\ & \\ & =0.46 \end{aligned}$ | $\begin{gathered} \hline \text { M1 } \\ \text { A1 } \\ 2 \end{gathered}$ |  |
| 13. (a) 8 <br> (b) $0.22 \ldots$ or 0.2 <br> (c) (i) $1 / 4$ or 0.25 <br> (ii) 1 | $\begin{gathered} \text { B1 } \\ \\ \text { B1 } \\ \text { B1 } \\ \text { B1 } \\ 4 \end{gathered}$ | Needs to show recurring, do not accept 0.2 or 0.22 etc |
| $\text { 14. } \begin{aligned} & \mathrm{m}=2 \\ & \mathrm{c}=4 \\ & \mathrm{y}=2 x+4 \end{aligned}$ | $\begin{gathered} \hline \text { B1 } \\ \text { B1 } \\ \text { B1 } \\ 3 \end{gathered}$ | Gradient <br> Intersection with $y-$ axis CAO |
| 15. (a) Group A with valid reason <br> (b) (About) 8 (minutes) | $\begin{gathered} \hline \text { B2 } \\ \text { B1 } \\ 3 \end{gathered}$ | Valid reason includes finished first, or median lower. B1 for Group A with incorrect or no reason. |
| 16. (a) $\begin{aligned} & 6 / 4 \times 3.2 \\ & =4.8(\mathrm{~cm}) \end{aligned}$ <br> (b) $\begin{aligned} & 4.5 / 6 / 4 \\ & =3(\mathrm{~cm}) \end{aligned}$ | $\begin{gathered} \text { M1 } \\ \text { A1 } \\ \text { M1 } \\ \text { A1 } \\ 4 \end{gathered}$ | Or equivalent <br> Or equivalent <br> If no marks in (a) or (b) then award SC 1 for sight of $6 / 4$ or 1.5 or $4 / 6$ or $2 / 3$ or 0.33 .. |


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| 17. $x^{2}+6 x-16$ | $\begin{gathered} \text { B2 } \\ 2 \\ \hline \end{gathered}$ | B1 for $x^{2}-16$ or for $6 x$. Only award B2 for the trinomial |
| 18. Correctly setting up 2 eqns for eliminating 1 variable <br> First variable's value Correctly substituting their first variable Second variable's value | $\begin{gathered} \text { M1 } \\ \text { A1 } \\ \text { M1 } \\ \text { A1 } \\ 4 \\ \hline \end{gathered}$ | Or alternate substitution method Either $x=5$ or $\mathrm{y}=-3$ FT their first variable FT their first variable |
| 19. (a) $\begin{aligned} & 5 x+5 y=8 y+5 \\ & 5 x=3 y+5 \\ & x=(3 y+5) / 5 \end{aligned}$ <br> (b) $\begin{aligned} & 10 \mathrm{k}-5 \mathrm{~m}=\mathrm{ck}+5 \\ & 10 \mathrm{k}-\mathrm{ck}=5 \mathrm{~m}+5 \\ & \mathrm{k}(10-\mathrm{c})=5 \mathrm{~m}+5 \\ & \mathrm{k}=(5 \mathrm{~m}+9) /(10-\mathrm{c}) \end{aligned}$ | $\begin{aligned} & \text { B1 } \\ & \text { B1 } \\ & \text { B1 } \\ & \text { B1 } \\ & \text { B1 } \\ & \text { B1 } \\ & \text { B1 } \\ & 7 \\ & \hline \end{aligned}$ | Expand FT each stage for equivalent <br> level of difficulty <br> Collect  <br> Divide Penalise -1 in (a) \& -1 (b) for <br> Expand <br> Collect <br> farther incorrect work  <br> Factorise  |
| $\text { 20. } \begin{aligned} & (3 x \quad 1)(2 x \quad 3) \text { or }\left(\begin{array}{lll} 3 x & 3 \end{array}\right)\left(\begin{array}{ll} 2 x & 1 \end{array}\right) \\ & (3 x+1)(2 x+3) \\ & x=-1 / 3 \text { and } x=-3 / 2 \end{aligned}$ | $\begin{gathered} \text { M1 } \\ \text { A1 } \\ \text { B1 } \\ 3 \\ \hline \end{gathered}$ | FT their pair of brackets. Ignore incorrect simplification Use of quadratic formula no marks |
| 21. (a) $\mathrm{g} \alpha \mathrm{~h}^{2} \text { or } \mathrm{g}=\mathrm{kh}^{2}$ $\begin{aligned} & 1=\mathrm{k} 3^{2} \\ & \mathrm{~g}=1 / 9 \mathrm{~h}^{2} \end{aligned}$ <br> (b) $4 / 9$ | $\begin{gathered} \text { M1 } \\ \text { M1 } \\ \text { A1 } \\ \text { B1 } \\ 4 \\ \hline \end{gathered}$ | FT $\mathrm{g} \alpha 1 / \mathrm{h}^{2}$ only, for all parts Maybe implied by use in (b) <br> FT their $\mathrm{g}=\mathrm{kh}{ }^{2}$ or $\mathrm{g}=\mathrm{k} / \mathrm{h}^{2}$ only |
| 22. $x=0.3444 \ldots$ and $10 x=3.444 \ldots$ and attempt to subtract $31 / 90$ | $\begin{gathered} \text { M1 } \\ \text { A1 } \\ 2 \end{gathered}$ | Or equivalent, e.g. Subtracting $10 x \& 100 x$ N.B. 3.1/9 gets M1, A0 |
| 23. (a) $\begin{aligned} & 5 / 11 \times 4 / 10 \\ & =2 / 11\end{aligned}$ <br> (b) Complete method, e.g. $\mathrm{P}\left(\mathrm{B}^{\prime} \mathrm{B}^{\prime}\right)$ $\begin{aligned} & (=7 / 11 \times 6 / 10) \\ & =21 / 55 \end{aligned}$ | $\begin{gathered} \text { M1 } \\ \text { A1 } \\ \text { M1 } \\ \text { A1 } \\ 4 \end{gathered}$ | Or equivalent (e.g. 20/110) <br> Or correct full listing with colours Or equivalent (e.g. 42/110) |
| 24. (a) (i) Correct sketch <br> (ii) Correct sketch <br> (b) Shift down <br> Correct shift down with $\mathrm{y}=-3$ indicated | $\begin{gathered} \text { B1 } \\ \text { B1 } \\ \text { M1 } \\ \text { A1 } \\ 4 \end{gathered}$ | May still be above the x -axis |
| 25. $6(x+5)+3(4 x-3)$ as a numerator $(4 x-3)(x+5)$ as a denominator $\begin{aligned} & 6 x+30+12 x-9 \\ & \frac{18 x+21}{(4 x-3)(x+5)} \end{aligned}$ | $\begin{gathered} \text { B1 } \\ \text { B1 } \\ \text { M1 } \\ \text { A1 } \\ 4 \end{gathered}$ | Brackets maybe implied by later working <br> Or $\frac{3(6 x+7)}{(4 x-3)(x+5)}$ Ignore incorrect expansion of $(4 x-3)(x+5)$ <br> Penalise further foolishness -1 |
| 26. $30+6 \sqrt{ } 2+5 \sqrt{ } 2+2$ <br> $=32+11 \sqrt{ } 2$ and irrational | $\begin{gathered} \text { M1 } \\ \text { A1 } \\ 2 \\ \hline \end{gathered}$ | $\sqrt{2} \sqrt{2}$ must be evaluated |


| GCSE Pilot 2006 Mathematics Higher Tier Paper 2 | Mark | Mark Scheme Comments |
| :---: | :---: | :---: |
| 1. A stage of working, e.g. $1 \frac{1}{2}$ (jars) to 2(slices), 3:4, $3 / 4$ 15 (jars) | $\begin{gathered} \text { M1 } \\ \text { A1 } \\ 2 \end{gathered}$ |  |
| 2. (a) 15 and 27 entered in the table <br> (b) $-1, \times 3$ or $x 3,-3$ | B1 <br> B2 $3$ | B1 for either $-1,-3$ or $x 3$ in either box Accept equivalent in words |
| 3. (a) (i) $150 \times 4+120(x 1)$ or <br> (ii) $150 \times 3+120 \times 2$ <br> $720(\mathrm{p})$ or (£)7.20 <br> $690(\mathrm{p})$ or (£)6.90 <br> (b) $72(\mathrm{p})$ or $69(\mathrm{p})$ or $3(\mathrm{p})$ <br> $720+72$ or $690+69$ or $30+3$ <br> $33(\mathrm{p})$ and Bonus (deal) | $\begin{aligned} & \text { M1 } \\ & \text { A1 } \\ & \text { A1 } \\ & \\ & \text { M1 } \\ & \text { M1 } \\ & \text { A1 } \\ & \\ & 6 \end{aligned}$ | Seen or implied in either part <br> Do not penalise decimal money notation <br> SC1 for (£)14 \& (£)11 <br> For finding a correct $10 \%$. FT from (a) Method of finding $110 \%$. FT from (a) Correct for FT for Mega \& Bonus logic Penalise place value of money overall $\mathbf{- 1}$ (e.g. all values which are pence with $£$ sign) |
| 4. $\begin{aligned} & 8 x+4 x=7-4 \\ & 12 x=3 \\ & x=3 / 12 \quad(=1 / 4=0.25) \end{aligned}$ <br> (b) $\begin{array}{lll} 10 x-15=50 & \text { or } & 2 x-3=50 / 5 \\ 10 x=65 & \text { or } & 2 x=13 \\ x=65 / 10 & \text { or } & x=13 / 2(=6.5) \end{array}$ <br> (c) (i) $2 x(x-3)$ <br> (ii) $3(a-4)$ <br> (d) $-2,1,6$ | $\begin{aligned} & \text { B1 } \\ & \text { B1 } \\ & \text { B1 } \\ & \text { B1 } \\ & \text { B1 } \\ & \text { B1 } \\ & \text { B2 } \\ & \text { B1 } \\ & \text { B2 } \\ & \hline 11 \end{aligned}$ | FT until $2^{\text {nd }}$ error in (a) \& (b) <br> B1 for partially factorised $2\left(x^{2}-3 x\right)$ or $x(2 x-6)$ or $2 x(x \ldots)$ or $2 x(\ldots-3)$ <br> B1 for any 2 terms correct OR SC1 for $-3,-2,-1$ |
| 5. Attempt substitution of one value of $x$ between 0 \& 4 <br> Two correct points on the line given (or plotted) <br> Correct straight line drawn | $\begin{gathered} \text { M1 } \\ \text { A1 } \\ \text { A1 } \\ 3 \end{gathered}$ | CAO. SC1 for $y=2 x+3$ or a straight line with correct gradient of 3 |
| 6. $20(\mathrm{~km} / \mathrm{h})$ | $\begin{gathered} \hline \text { B2 } \\ 2 \end{gathered}$ | B1 for sight of 30 and $11 / 2$ (or 1 hr 30 mins or 90 min ) (NOT 1.30hr). SC1 for 12 (from 30/2.5) |
| 7. (a) 4.8 <br> (b) $3 / 4$ or 0.75 <br> (c) 6.14 <br> (d) 945 and 955 | B2 <br> B1 <br> B2 <br> B2 <br> 7 | B1 for $4.809 \ldots$ or SC1 for -1.8 or their answer to 1 dp . <br> B1 for 6.1(3652....) <br> B1 each. Accept 954.9999... etc, not 954.9 . |

\begin{tabular}{|c|c|c|}
\hline GCSE Pilot 2006 Mathematics Higher Tier Paper 2 \& Mark \& Mark Scheme Comments \\
\hline 8. \(\begin{array}{llll} \& 5500.00 \& \& \\ \& \underline{330.00} \& \& \\ \& 5830.00 \& \& \\ \& \underline{349} .8(0) \& \underline{\mathrm{OR}} \& \\ \& \& 6179.8(0) \& 5179.8(0) \\ \& \& \text { A1 }\end{array}\) \& \[
\begin{aligned}
\& \text { B1 } \\
\& \text { M1 } \\
\& \text { A1 }
\end{aligned}
\] \& \begin{tabular}{l}
For a correct 6\%. \\
For the overall method (2 stages of adding different 6\%). \\
C.A.O. Ignore subsequent working. SC1 for (£)6160 (simple interest), alternatively they may get the B1 for ( \(\mathfrak{£}\) )660 if seen.
\end{tabular} \\
\hline 9. Mid points \(154,161,168\)
\[
\begin{aligned}
\& 154 \times 18+161 \times 37+168 \times 25 \\
\& \left(\sum f x=\right) 12929 \\
\& 161.6(125)
\end{aligned}
\] \& \[
\begin{aligned}
\& \text { B1 } \\
\& \text { M1 } \\
\& \text { A1 } \\
\& \text { A1 }
\end{aligned}
\] \& FT for their mid points from within group (not bounds) FT for correct sum of their \(f x\) terms FT their \(\sum f x / 80\) correct evaluated. Do not allow 161. Unsupported 161.6125 awarded all 4 marks. SC1 for bounds with correct FT answer (lower 158.6125, upper 164.6125) \\
\hline \begin{tabular}{l}
10. (a)
\[
\begin{aligned}
\& 1 / 2 \times \prod^{\times} \times 6.4^{2} \\
\& =64 .\left(33 \ldots \mathrm{~cm}^{2}\right)
\end{aligned}
\] \\
(b) Area \(\times\) length \(=2.5 \times 1.6 \times(100)\) Change of units, e.g. 160 or \(\times 100\) shown \(=400\left(\mathrm{~cm}^{3}\right)\)
\end{tabular} \& \[
\begin{gathered}
\text { M1 } \\
\text { A1 } \\
\text { M1 } \\
\text { M1 } \\
\text { A1 } \\
5
\end{gathered}
\] \& \begin{tabular}{l}
SC1 for 128. (...), 257. (...) \\
Change of units not necessarily shown. \\
CAO
\end{tabular} \\
\hline \begin{tabular}{l}
11. One correct evaluation
\[
1 \leq x \leq 2
\] \\
2 correct evaluations, \\
\(1.3 \leq x \leq 1.6\), one either side of 0 \\
2 correct evaluations, \\
\(1.45 \leq x \leq 1.5\), one either side of 0 \\
OR correct evaluation of 1.45 if previous \\
B1 awarded \\
1.5 \\
No calculations shown: accept "too high",">", etc.
\end{tabular} \& B1

B1
M1

A1

4 \& | $X$ | $2 x^{3}+x-8$ |  |
| :--- | :--- | :--- |
| 1 | -5 |  |
| 2 | 10 |  |
|  |  |  |
| 1.3 | -2.306 |  |
| 1.4 | -1.112 |  |
| 1.5 | 0.25 |  |
| 1.6 | 1.792 |  |
|  |  |  |
| 1.45 | -0.45275 |  |
| 1.46 | -0.315728 |  |
| 1.47 | -0.176954 |  |
| 1.48 | -0.036416 |  |
| 1.49 | 0.105898 |  | <br>

\hline | 12. |
| :--- |
| (a) $\begin{aligned} & (x-10)(x+1) \\ & x=10 \text { and } x=-1 \end{aligned}$ |
| (b) $\begin{aligned} & 24-2 x=30-5 x \\ & 3 x=6 \\ & x=6 / 3(=2) \end{aligned}$ |
| (c) $12 x^{8} y^{7}$ |
| (d) $(x+3)(x-3)$ | \& \[

$$
\begin{gathered}
\hline \text { B2 } \\
\text { B1 } \\
\text { B1 } \\
\text { B1 } \\
\text { B1 } \\
\text { B2 } \\
\\
\text { B1 } \\
9 \\
\hline
\end{gathered}
$$

\] \& | B1 for $\left(\begin{array}{lll}x & 10\end{array}\right)\left(\begin{array}{ll}x & 1\end{array}\right)$ with no or incorrect signs B1 their pair of brackets |
| :--- |
| FT (including $24-2 x=30-x$ to $-x=6$ here) |
| FT (from above to $x=-6$ ) |
| B1 for any two factors number, $x \& y$ correct, or correct but with "times" left in expression |
| FT until $2^{\text {nd }}$ error | <br>

\hline
\end{tabular}

| GCSE Pilot 2006 Mathematics Higher Tier Paper 2 | Mark | Mark Scheme Comments |
| :---: | :---: | :---: |
| 13. (a) $0.3,0.8,0.2,0.8$ on correct branches <br> (b) $0.7 \times 0.8$ <br> $=0.56$ | $\begin{gathered} \mathrm{B} 2 \\ \\ \text { M1 } \\ \text { A1 } \\ 4 \\ \hline \end{gathered}$ | B1 for one correct entry <br> FT their 0.8 entry |
| 14. (a) (i) $6 \times 10^{6}$ <br> (ii) $4.3 \times 10^{-3}$ <br> (b) $1.68 \times 10^{9}$ | $\begin{aligned} & \text { B1 } \\ & \text { B1 } \\ & \text { B2 } \\ & \\ & \hline \end{aligned}$ | Penalise -1 once only for incorrect notation <br> Allow $1.7 \times 10^{9}$ for B2 <br> B1 for $16.8 \times 10^{8}$ OR $n \times 10^{9}$ where $n=8.4 \times 2 / 10$ incorrectly evaluated OR 1680000000 OR $1.6 \times 10^{9}$ |
| 15. (a) $\begin{aligned} & \cos 39^{\circ}=\mathrm{EF} / 14.8 \\ & \mathrm{EF}=11.5(0 \ldots)\end{aligned}$ $\mathrm{EF}=11.5(0 \ldots)$ <br> (b) $\tan \mathrm{S}=12.8 / 18.5$ <br> $\mathrm{S}=34.679$ rounded or truncated to at least 1 d.p. or $35^{\circ}$ | $\begin{gathered} \text { M1 } \\ \text { A2 } \\ \\ \text { M1 } \\ \text { A2 } \\ 6 \end{gathered}$ | A 1 for $\mathrm{EF}=14.8 \times \cos 39^{\circ}$ <br> A1 for $\tan \mathrm{S}=0.69(189 \ldots)$. |
| $\text { 16. } \begin{aligned} & x=\left\{-31 \pm \sqrt{ }\left(31^{2}-4 \times 3 \times 8\right) \quad\right\} /(2 \times 3) \\ & =(-31 \pm \sqrt{865) / 6} \\ & x=-0.26 \text { and } \times=-10.07 \end{aligned}$ | $\begin{gathered} \text { M1 } \\ \text { M1 } \\ \text { A1 } \\ \\ \hline \end{gathered}$ | Allow one slip in substitution <br> FT if M1 awarded and denominator treated as 2a for numerator |
| 17. Attempt to calculate at least 1 area with at least 1 correct Calculate shown or implied for all 6 areas, with at least 4 correct 63 | $\begin{gathered} \text { M1 } \\ \text { M1 } \\ \text { A1 } \\ 3 \end{gathered}$ | $\begin{aligned} & \text { Areas are } 1.5 \times 10+2 \times 6+4 \times 2.5+4 \times 3+6 \times 1.5+10 \times 0.5 \\ & =15+12+10+12+9+5 \end{aligned}$ |
| 18. Mean $=5.22$ $\sum x^{2}=320.54$ or sight of complete correct method $\text { S.D. }=2.19(2 \ldots) \text { or } 2.2$ | $\begin{gathered} \mathrm{B} 1 \\ \text { M1 } \\ \text { A1 } \\ \\ \hline \end{gathered}$ | Or sight 4.79(...) |
| 19. (a) $90^{\circ}$ <br> (b) $62^{\circ}$ <br> (c) angle in semi circle OR (b) alternate segment theorem | $\begin{gathered} \text { B1 } \\ \text { B1 } \\ \text { E1 } \\ 3 \end{gathered}$ | OR equivalent description or calculations |
| $\text { 20. } \begin{gathered} 1 / 2 \times 4 / 3 \pi \mathrm{r}^{3}=34.2 \text { or equivalent } \\ \mathrm{r}^{3}=\frac{6 \times 34.2}{4 \pi} \quad(=16.329 \ldots) \\ \mathrm{r}=2.5(37 \ldots) \end{gathered}$ | $\begin{gathered} \text { M1 } \\ \text { M1 } \\ \text { A1 } \\ \hline \end{gathered}$ | Maybe implied in stages of working <br> SC1 for 2.01(3...) from using volume of a sphere |
| 21. $\begin{array}{ll}11.5^{\circ} \\ & 168.46^{\circ} \text { or } 168.5^{\circ}\end{array}$ | $\begin{gathered} \text { B1 } \\ \text { B1 } \\ 2 \end{gathered}$ | FT 180 - first value. Penalise further values - only |


| GCSE Pilot 2006 Mathematics Higher Tier Paper 2 | Mark | Mark Scheme Comments |
| :---: | :---: | :---: |
| 22. (a) $\begin{aligned} & 10 x+3 y-(4 x+y) \\ & =6 x+2 y\end{aligned}$ <br> (b) $\begin{aligned} & \mathbf{A C}=9 \boldsymbol{x}+3 \mathbf{y} \\ & \mathbf{O C}=13 \boldsymbol{x}+4 \mathbf{y} \end{aligned}$ | $\begin{gathered} \text { M1 } \\ \text { A1 } \\ \text { M1 } \\ \text { A1 } \\ 4 \end{gathered}$ | Award SC1 for $6 \boldsymbol{x}+4 \mathbf{y}$ from $10 x+3 \mathbf{y}-4 \boldsymbol{x}+\mathbf{y}$ <br> FT their $1.5 \times$ (a) in the form $\ldots \boldsymbol{x}+\ldots \mathbf{y}$. Accept unsimplified form <br> Accept unsimplified form. FT their $1.5(\mathrm{a})+4 \boldsymbol{x}+\mathbf{y}$ |
| $\text { 23. } \begin{aligned} & \mathrm{BD}^{2}=26.2^{2}+29.3^{2}-2 \times 26.2 \times 29.3 \times \cos 30^{\circ} \\ & =215.3(038 . .) \\ & \mathrm{BD}=14.67(\ldots) \text { or } 14.7 \\ & \quad \frac{14.4}{\sin 50^{\circ}}=\frac{\mathrm{BD}}{\sin \mathrm{~A}} \\ & \sin \mathrm{~A}=\mathrm{BD} \times \sin 50^{\circ} / 14.4 \\ & 51.29(79 \ldots)^{\circ} \text { or } 51.3^{\circ} \text { or } 51.4^{\circ} \end{aligned}$ | M1 M1 A1 M1 M1 A1 6 | FT their BD |

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